

# *Hansen Solubility Parameters: Introduction and Applications*

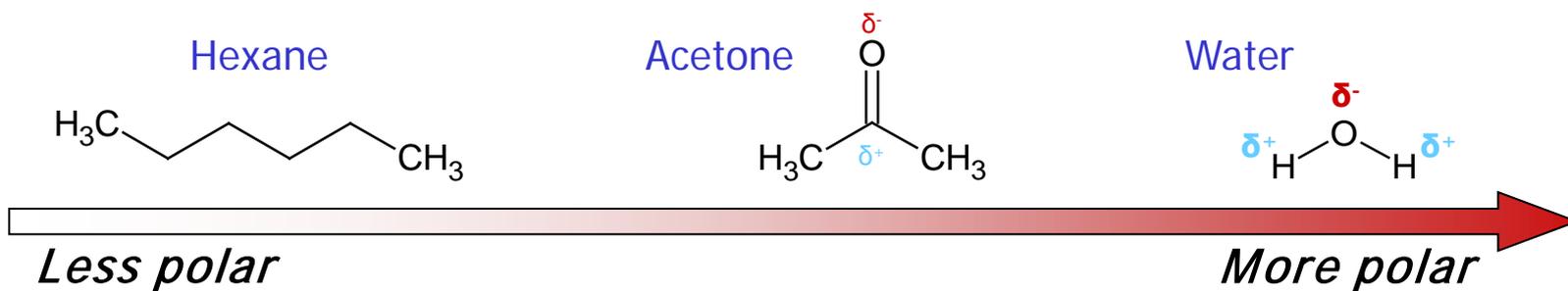
---

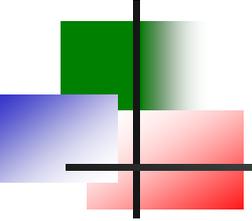
**Assoc. Prof. Daniel F. Schmidt**  
*Department of Plastics Engineering*



# Solubility

- How do we understand solubility?
  - "Like dissolves like"
  - Polar vs. non-polar solvents
    - Typically refers to the degree of charge separation in the solvent molecule
    - The greater the strength and / or separation of charges, the more polar the solvent

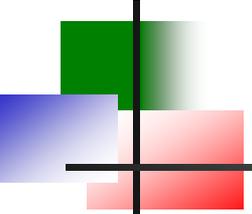


A decorative graphic consisting of overlapping colored squares (green, blue, red) and a black crosshair.

# Quantifying Behavior

---

- **If we want to be quantitative, there are several approaches; two examples:**
  - **Kauri-butanol (K<sub>b</sub>) value (ASTM D1133)**
    - Indicates maximum amount of compound that can be added to solution of kauri resin (resin from the kauri tree of New Zealand) in butanol without causing cloudiness
  - **Octanol-water partition coefficient (K<sub>OW</sub> or log P) (ASTM E1147)**
    - High values indicate compound prefers octanol phase (less polar)
    - Low values indicate compound prefers water phase (more polar)



# Quantifying Behavior

---

- **Can also make a thermodynamic argument – for example, based on the removal of a single molecule from a material**
  - **Must overcome all intermolecular interactions (“stickiness”) between molecule and its neighbors to do this**
  - **This occurs during vaporization, and also during dissolution**
  - **Prof. Joel Henry Hildebrand (UC Berkeley Chemistry) proposed this treatment**
  - **Hildebrand solubility parameter defined as the square root of the aforementioned quantity (the cohesive energy density)**

# Hildebrand Solubility Parameter

Hildebrand solubility parameter  
[typical units are  
(cal/cm<sup>3</sup>)<sup>1/2</sup> or MPa<sup>1/2</sup>]

Heat of vaporization of  
compound (energy/mol)

Thermal energy  
available at a  
given temperature  
(energy/mol)

$$\delta = \sqrt{CED} = \sqrt{\frac{\Delta H_v - RT}{V_m}}$$

Cohesive  
energy density  
of compound  
("molecular  
stickiness",  
energy/volume)

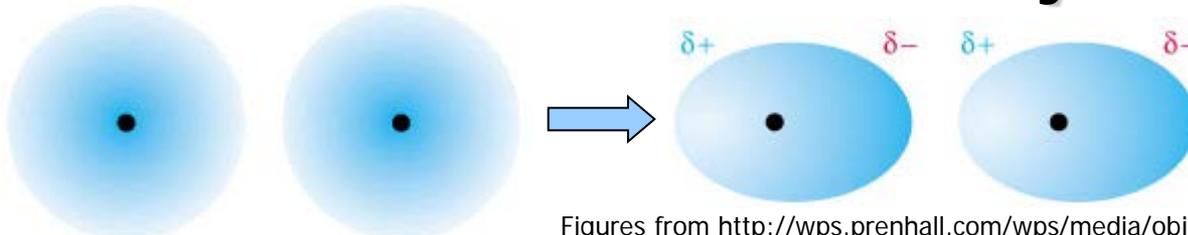
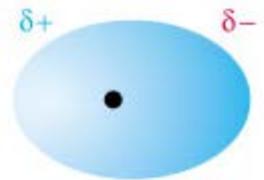
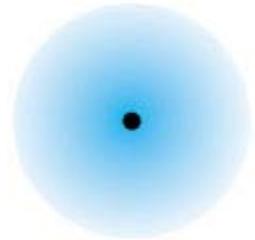
Molar volume  
of compound  
(volume/mole)

Hardest thing to  
find is the heat of  
vaporization of a  
compound (think  
about plastics!)

# What contributes to molecular "stickiness"?

## ■ Dispersion Forces

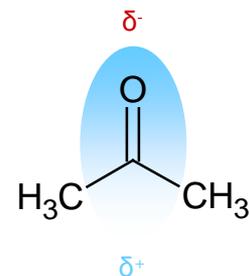
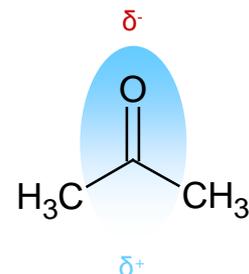
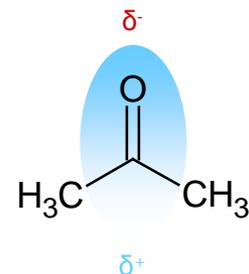
- All atoms are surrounded by electron "clouds"
- The electron cloud is, on average, evenly distributed around the atom
- At a given instant, however, the electron distribution may be lopsided
- This temporary polarization results in attractive interactions with nearby atoms



# What contributes to molecular "stickiness"?

## ■ Polar interactions

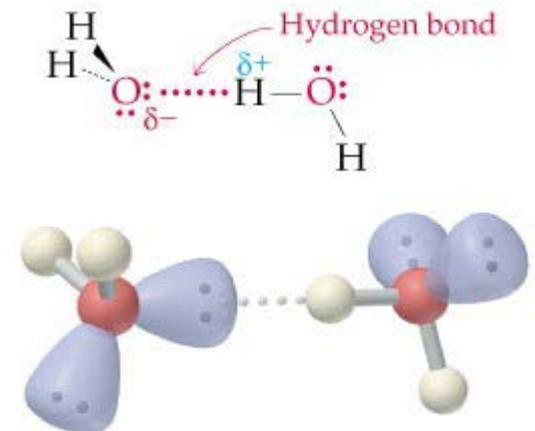
- Some atoms have a greater affinity for electrons than others (more electronegative)
- Bonds between atoms of differing electronegativities are polarized as a result
- Dipoles thus formed attract one another
- Same idea as with dispersion forces, but dipoles are permanent, not temporary



# What contributes to molecular "stickiness"?

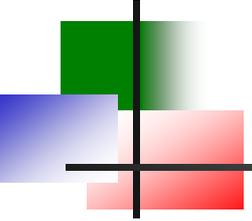
## ■ Hydrogen bonding

- Hydrogen has just one electron, so when electron density is pulled away from hydrogen (i.e. by an electronegative atom), the nucleus is exposed
- This results in exceptionally strong polar interactions with other atoms possessing extra lone pairs of electrons
- As with previous cases, the interaction is electrostatic in nature (opposites attract)



# Shortcomings of a single parameter approach

- The Hildebrand solubility parameter can be useful, but it does not account for the origins of molecular “stickiness” (or their consequences)
  - This means it is possible for various combinations of intermolecular interactions to give rise to the same Hildebrand solubility parameter
  - EXAMPLE: nitroethane and 1-butanol have the same Hildebrand solubility parameter ( $\sim 23 \text{ MPa}^{1/2}$ ); neither will dissolve epoxy resin alone, but a blend of the two will
- Hildebrand recognized this, and tried to address it by further classifying compounds according to hydrogen bonding ability (weak, moderate, strong), but this approach has limited utility



# Accounting for interactions: Hansen Solubility Parameters

---

- Hansen solubility parameters address this issue by specifying separate quantities for each of the three aforementioned intermolecular forces:
  - $\delta_d$  – Dispersion parameter
  - $\delta_p$  – Polar parameter
  - $\delta_h$  – Hydrogen-bonding parameter
- Can still define total solubility parameter ( $\delta_{\text{total}}^2 = \delta_d^2 + \delta_p^2 + \delta_h^2$ ), but can separate cohesive energy density by interaction type

# Thinking about Hansen Solubility Parameters (HSPs)

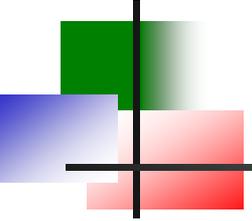
- HSPs mean we can represent each compound as a point in 3D "solubility space"
- Distance between HSP points in solubility space is defined as follows:

$$R_a^2 = 4(\delta_{d1} - \delta_{d2})^2 + (\delta_{p1} - \delta_{p2})^2 + (\delta_{h1} - \delta_{h2})^2$$

- With some work, it is also possible to define an interaction radius ( $R_0$ ) and a reduced energy difference ( $RED = R_a/R_0$ )
  - $RED > 1 \rightarrow$  Incompatible,  $RED < 1 \rightarrow$  Compatible

# Thinking about Hansen Solubility Parameters (HSPs)

- In some cases, HSP values are intuitive
  - Hydrocarbons are dominated by  $\delta_d$
  - Water is dominated by  $\delta_h$
  - Similar compounds will have similar HSPs (for example, *n*-butanol will be similar to *n*-propanol)
- HSPs can be correlated with other properties
  - Strong correlation between refractive index and  $\delta_d$
  - Strong correlation between dipole moment and  $\delta_p$
  - Strong correlation between surface energy and a mix of parameters plus molar volume
- Not perfect
  - Molecular size and shape are not captured
  - Some interaction types are ignored (ion-dipole for example)
- Nevertheless, "good enough" to give reasonable predictions



# Defining HSPs: Group Contributions

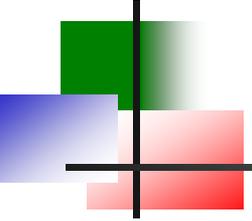
---

- Break molecule into functional groups
- Add up the  $\delta_d$ ,  $\delta_p$ , and  $\delta_h$  contributions from each group to generate estimate
- Van Krevelen, Hoy, Beerbower
  - Based on a restricted range of functional groups
  - Different starting values so different end results
- Stefanis-Panayiotou – more modern
- All require manual group assignment

# Hansen Solubility Parameters in Practice (HSPiP)

---

- **Software package developed by Hansen, Abbott and Yamamoto**
- **Able to provide HSPs for arbitrary molecules**
  - **Has a large look-up table for materials whose HSPs are known**
  - **Utilizes “Yamamoto Molecular Breaking” (Y-MB) model for other compounds**
    - **Carefully chosen / optimized set of functional groups**
    - **Sanity checking vs. other data sources (refractive index, dipole moment, surface tension, heat of vaporization)**
    - **Tested against “over-fitting”**
  - **Best estimate of HSPs available at the moment**
  - **HSPiP also automates aforementioned manual methods**



# Hansen Solubility Parameters in Practice (HSPiP)

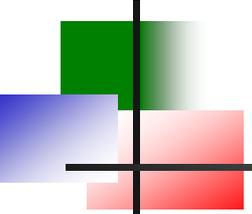
---

- **As HSPs are related to heat of vaporization, HSPiP can:**
  - **Estimate boiling point**
  - **Estimate vapor pressure**
  - **Estimate Antoine coefficients**
- **Melting point predictions are made independently using an external model based on an extensive validated melting point database**

# The Classic HSP Measurement Technique

---

- **The key to HSP's practical success**
- **Widely applicable**
  - Crystalline solids
  - Polymers
  - Nanoparticles
  - DNA
- **Take 20 test tubes, find if the stuff is "happy" in 20 different, representative, known solvents**
  - Set of solvents should neither be "all bad" or "all good"
  - Best to cover a decent range of HSP values with solvents
- **Plot the solubility sphere in 3D HSP solubility space**
  - Can define center of sphere (i.e. HSPs for "stuff")
  - Can define radius of sphere (i.e. interaction radius  $R_0$ )



# High Throughput Options

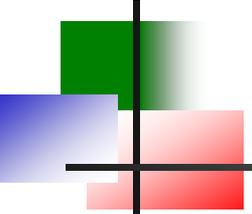
---

- **Assembling even 20 solvents can be a big barrier to HSP measurement**
- **Small labs /companies/universities may not want to do this**
- **Big companies have robots**
  - **All large HSPiP users have automated HSP determination systems**
    - **Some better than others**
    - **Some automate solubility measurements**
      - **Agfa-Gaevert, Belgium offering this as a service**
      - **Also VLCI in the Netherlands**

# High Throughput Example: VLCI

- **Chemspeed FORMAX unit enables automated high-throughput testing**





# Grid Technique

---

- Use 4 pairs of solvents
- Create a “grid” spanning the relevant solubility space
- Developed at U. Erlangen for organic photovoltaics
- Much easier with robotics
- Great for targeted measurements

## Determination of the P3HT:PCBM solubility parameters via a binary solvent gradient method: Impact of solubility on the photovoltaic performance

Florian Machui<sup>a,\*</sup>, Stefan Langner<sup>a</sup>, Xiangdong Zhu<sup>a</sup>, Steven Abbott<sup>b</sup>, Christoph J. Brabec<sup>a,c</sup>

<sup>a</sup> I-MEET (Institute Materials for Electronics and Energy Technology) University Erlangen-Nuremberg, Martensstrasse 7, 91058 Erlangen, Germany

<sup>b</sup> 7 Elsmere Road, Ipswich, Suffolk IP1 3SZ, United Kingdom

<sup>c</sup> Bavarian Center for Applied Energy Research (ZAE Bayern), Am Weichselgarten 7, 91058 Erlangen, Germany

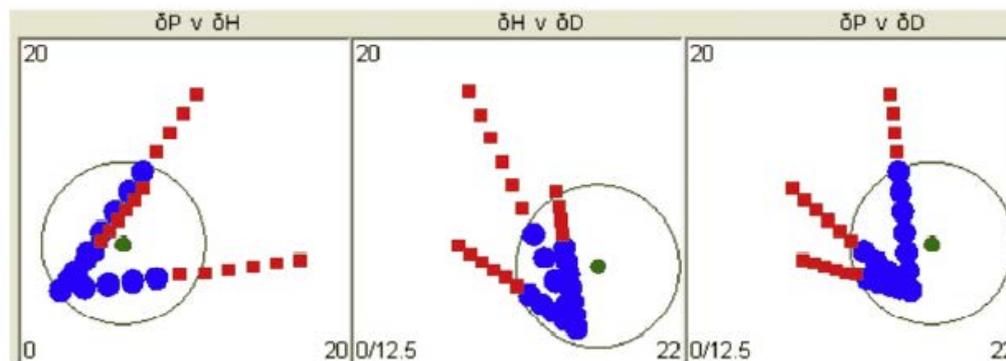
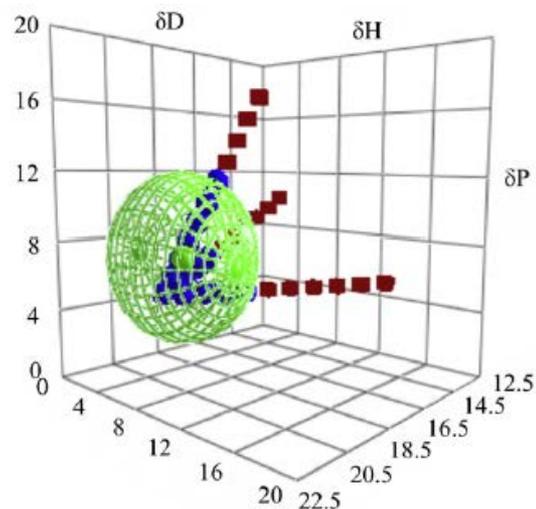
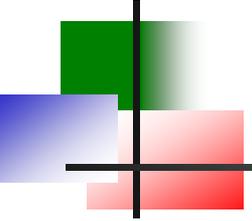


Fig. 4. HSP diagrams of PCBM: a) different solvents method and b) binary solvent gradient method with solubility limit  $5 \text{ mg mL}^{-1}$ .

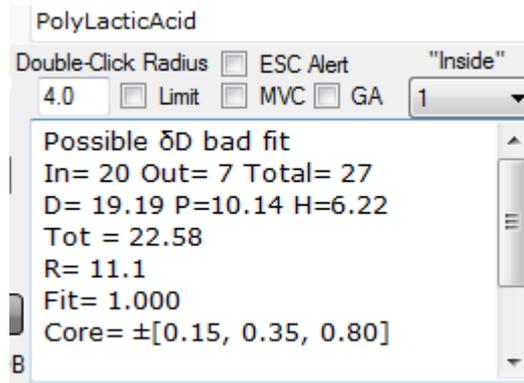


# Notes on Polymer Solubility

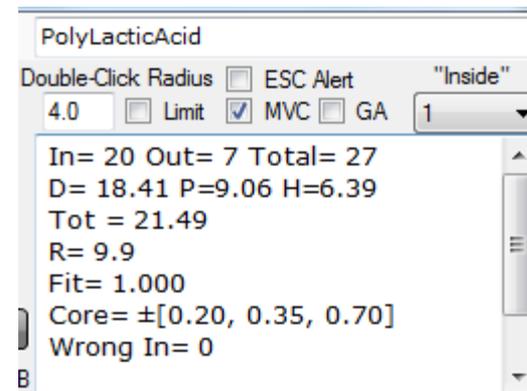
---

- **An important asymmetry**
  - A polymer can be rather insoluble in a solvent
  - The same solvent can be quite soluble in the polymer
- **This relates to the entropy of mixing**
  - Much more to be gained (entropically) dissolving small molecules than polymers
  - Likewise, semi-crystalline polymers resist dissolution all the more (greater “stickiness” between molecules in crystalline domains)
    - For example, polyethylene and polypropylene dissolve in hydrocarbons (as predicted by HSP values) – but only at elevated temperatures

# HSPiP Refinements: Molar Volume Correction (MVC)



**Classic fit – size of solvent not included**

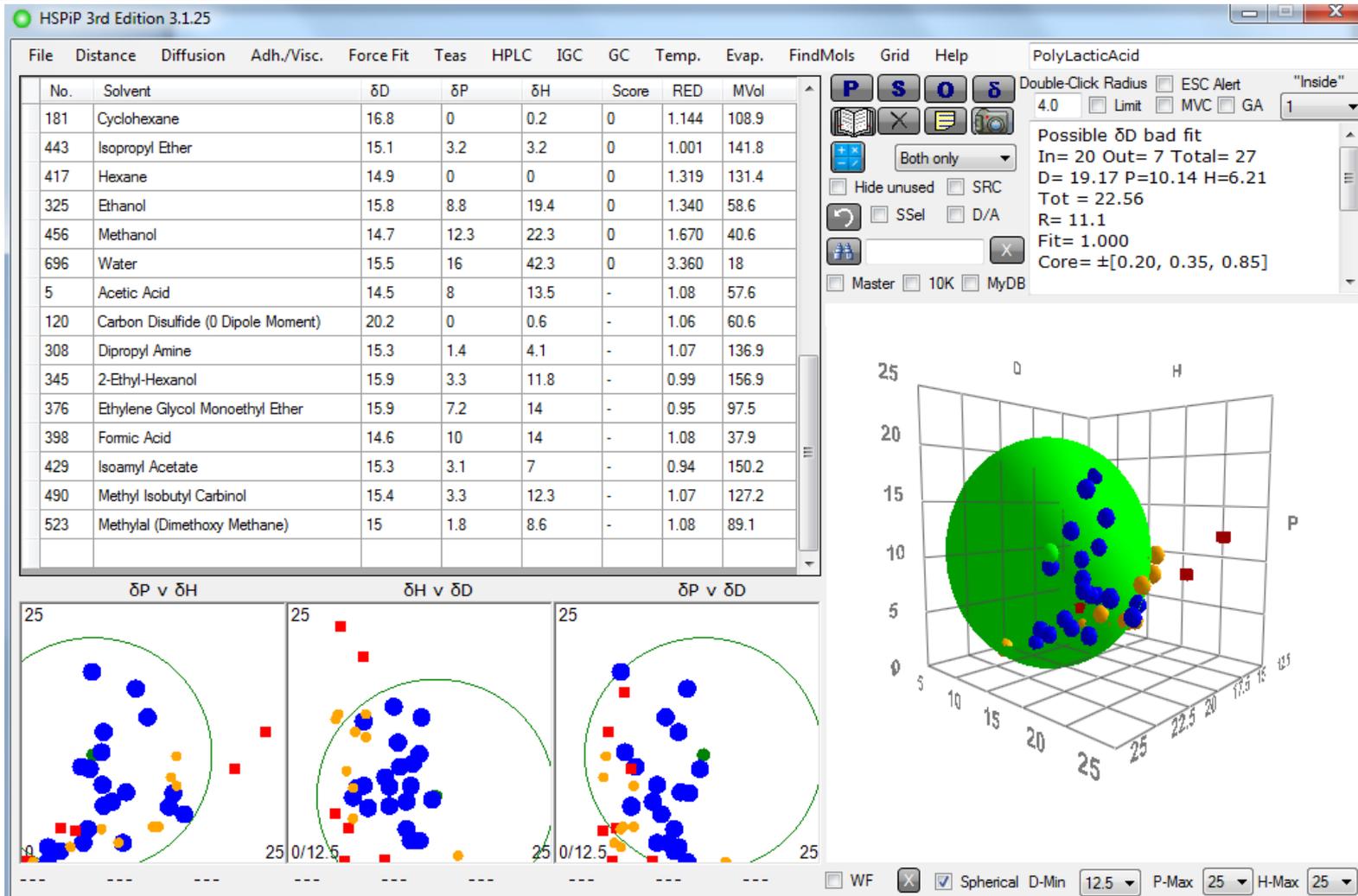


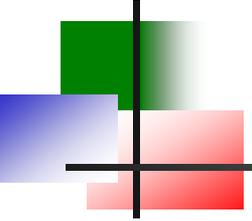
**MVC fit – small solvents “penalized”, large solvents “accommodated”**

# HSPiP Refinements: Solvent Range Check (SRC)

Identifies solvents at the edge of the apparent solubility sphere

These improve fits the most with the least effort





# HSPiP Refinements: Hydrogen Bond Donors and Acceptors

---

- Divide  $\delta_h$  into hydrogen bond donor and acceptor components
- Allows for specific interactions that might increase solubility, such as C=O acting as acceptor and -OH as donor
- Careful analysis shows it's important
  - So far not a great success for normal fits
  - Continuing development work

# HSPiP Refinements: Accounting for Temperature

Thermal expansion reduces cohesive energy density

HSP values decrease as a result

Accounted for by indicating CTE

HSPiP 3rd Edition 3.1.25

Force Fit	Teas	HPLC	IGC	GC	Temp.	Evap.	FindMols	Grid	Help
$\delta D$	$\delta P$	$\delta H$	Score	RED	MVol				
19.0 -1.3	8.8 -0.2	5.9 -0.5	1	0.122	80.9				
18.0 -1.0	12.3 -0.3	7.2 -0.6	1	0.273	96.6				
17.0 -1.0	7.3 -0.2	7.1 -0.5	1	0.417	64.4				
18.1 -1.0	6.6 -0.1	9.3 -0.7	1	0.466	69.9				
16.0 -0.9	9.0 -0.2	5.1 -0.4	1	0.481	90.2				
16.8 -0.9	5.7 -0.1	8.0 -0.6	1	0.556	81.9				
17.8 -1.5	3.1 -0.1	5.7 -0.5	1	0.696	80.5				
15.5 -1.4	10.4 -0.4	7.0 -0.7	1	0.670	73.8				
17.4 -1.0	13.7 -0.3	11.3 -0.9	1	0.649	77.4				
18.4 -1.0	16.4 -0.4	10.2 -0.8	1	0.723	71.3				
17.5 -1.0	1.8 0.0	9.0 -0.7	1	0.850	85.7				
15.8 -1.3	5.3 -0.2	7.2 -0.6	1	0.752	98.6				
17.0 -1.6	1.8 -0.1	5.3 -0.5	1	0.882	73.1				
18.5 -0.8	6.5 -0.1	13.7 -1.0	1	0.796	105				
18.0 -1.2	1.4 0.0	2.0 -0.2	1	0.882	106.6				
17.8 -1.0	1.0 0.0	3.1 -0.2	1	0.885	121.1				

Temperature dialog box:  
 Temperature °C: 70  
 Default expansion coefficient: 0.0010  
 Quick Calculator:  
 $\delta D$ : 16.3,  $\delta P$ : 6.7,  $\delta H$ : 5.5 At T°C  
 $\delta D$ : 17.3,  $\delta P$ : 6.9,  $\delta H$ : 6.0 At 25°C  
 $\delta D$ : 16.0,  $\delta P$ : 5.0,  $\delta H$ : 5.0 At 25°C  
 $\delta D$ : 15.1,  $\delta P$ : 4.9,  $\delta H$ : 4.6 At T°C

3D Plot:  $\delta D$  vs  $\delta P$  vs  $\delta H$  showing a green sphere and blue/red points.

2D Plots:  $\delta H$  v  $\delta D$ ,  $\delta P$  v  $\delta D$

Summary: PolyLacticAcid  
 In= 20 Out= 7 Total= 27  
 D= 17.54 P=9.80 H=5.16  
 Tot = 20.74  
 R= 10.4  
 Fit= 1.000  
 Core= ±[0.15, 0.30, 0.85]  
 Wrong In= 0

# HSPiP Refinements: Fitting Solubility Data

HSPiP 3rd Edition 3.1.25

File Distance Diffusion Adh./Visc. Force Fit Teas HPLC IGC GC Temp. Evap. FindMols Grid Help

No.	Solvent	$\delta D$	$\delta P$	$\delta H$	Score	RED	MVol
1	ACN	15.3	18.0	6.1	2.08	1.898	53

An API w DMSO and 4 branches

Double-Click Radius  ESC Alert  
4.0  Limit  MVC  GA

In= 16 Out= 0 Total= 16  
D= 19.20 P=12.30 H=8.90  
Tot = 24.48  
R= 5.3  
Fit= 0.884

### Advanced Sphere Fitting

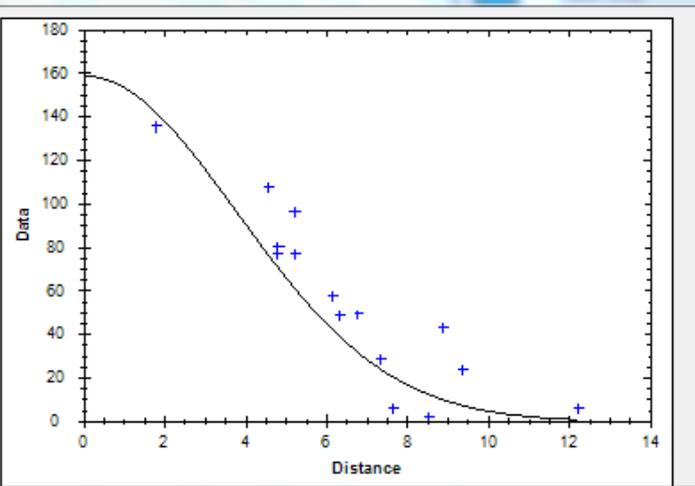
Classic GA  
 Double Sphere

"Inside"  Fitting Accuracy

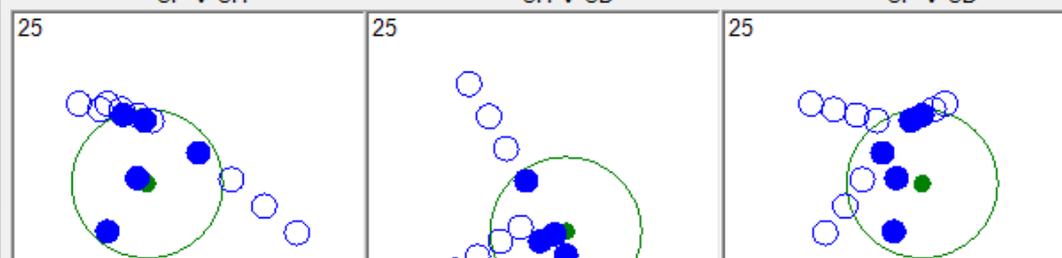
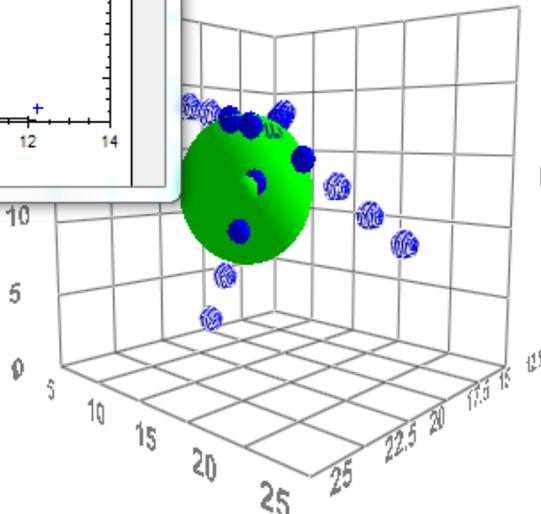
Use initial guess  
 $\delta D$   $\delta P$   $\delta H$   
 17.0 4.0 3.0

Data points  Good is small  Split High/Low @ 150.000  
 Radius for Data fit   Use Log fit  
 Fit to Exponential  MVC  Show Fit  Show Distance

Data fit results shown in main form



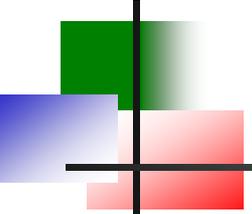
1	Propylene Carbonate	20.0	18.0	4.1	6.08	1.438	85
		$\delta P$ v $\delta H$		$\delta H$ v $\delta D$		$\delta P$ v $\delta D$	

# Special Topics: HSPs and Surfactants

---

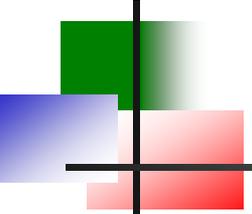
- They don't mix
- You *can* estimate or measure the HSP of a surfactant molecule – it's just an ordinary molecule
- Solubility parameter models in general (not just HSPs) assume that the same parameters apply everywhere ("mean field")
  - Cannot deal with situations where interactions are with specific parts of a molecule, molecules orient, etc.
  - This can be a problem when dealing with nanoparticles as well, i.e. if they possess multiple types of surfaces (modified or not, ends vs. sides, edges vs. faces, etc.)

A decorative graphic consisting of overlapping colored squares (green, blue, red) and a black crosshair.

# Special Topics: Stain Removal

---

- **No issues when using HSP to guide solvent selection for stain removal**
  - Important to keep in mind however that diffusion in is faster than diffusion out
  - That's why our plastic microwave dishes become stained over time
- **With surfactants, other models needed**
  - Ex. Hydrophilic-Lipophilic Difference - Net Average Curvature (HLD-NAC) model

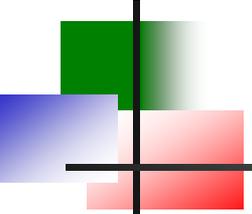
A decorative graphic consisting of overlapping colored squares (green, blue, red) and a black crosshair.

# Specific Topics: Solvent Blends

---

- A perfect HSP match with a perfect solvent (from the standpoint of cost, safety, vapor pressure, odor, regulatory approvals, etc.) is very rare (few new solvents)
- Can create blends to address this issue
- An X:Y mix of two solvents leads to an X:Y average of their HSPs (where X and Y are in vol%)
- You can even create a perfect solvent from a mix of two non-solvents
  - This was the proof of the power of HSP 40 years ago
  - Impossible to do with Hildebrand
- HSPiP can propose both binary and ternary blends, estimate and optimize evaporation rates

# Special Topics: Example of Rational Green Substitution

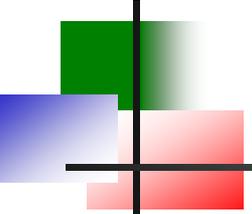
A decorative graphic consisting of overlapping colored squares (green, blue, red) and a black crosshair.

---

- FAME (Fatty Acid Methyl Esters) are not particularly good solvents, but are "green" [16.4, 2.6, 4.5]
- Glycerol carbonate comes from bio-glycerol, CO<sub>2</sub> (in principle) and is biodegradable – but is much too polar to be highly useful [17.9, 25.5, 17.4]
- A 60:40 mix is an impressive match for a great (but unusable) solvent like dimethyl acetamide (DMAc)

# Special Topics: HSPs and Biological Systems

- **Proteins, DNA bases exist in high HSP space (DNA bases → [19, 8, 8])**
  - **Chemicals that interact with and / or disrupt these biomacromolecules should have similar HSPs**
    - **Useful for identifying potentially cytotoxic and / or therapeutic agents**
- **Skin permeation is predicted in a much more nuanced manner than log  $K_{OW}$  method**
  - **DMSO is a good HSP match for skin; doesn't destroy it, permeates through it**
  - **Terpenes indicated as permeation enhancers, but this depends on what they're mixed with; 50:50 ethanol / terpenes gives HSP match with skin as well**
  - **Alternatively, stay away from [17,8,8] if you want to avoid skin permeation**

A decorative graphic consisting of overlapping colored squares (green, blue, red) and a black crosshair.

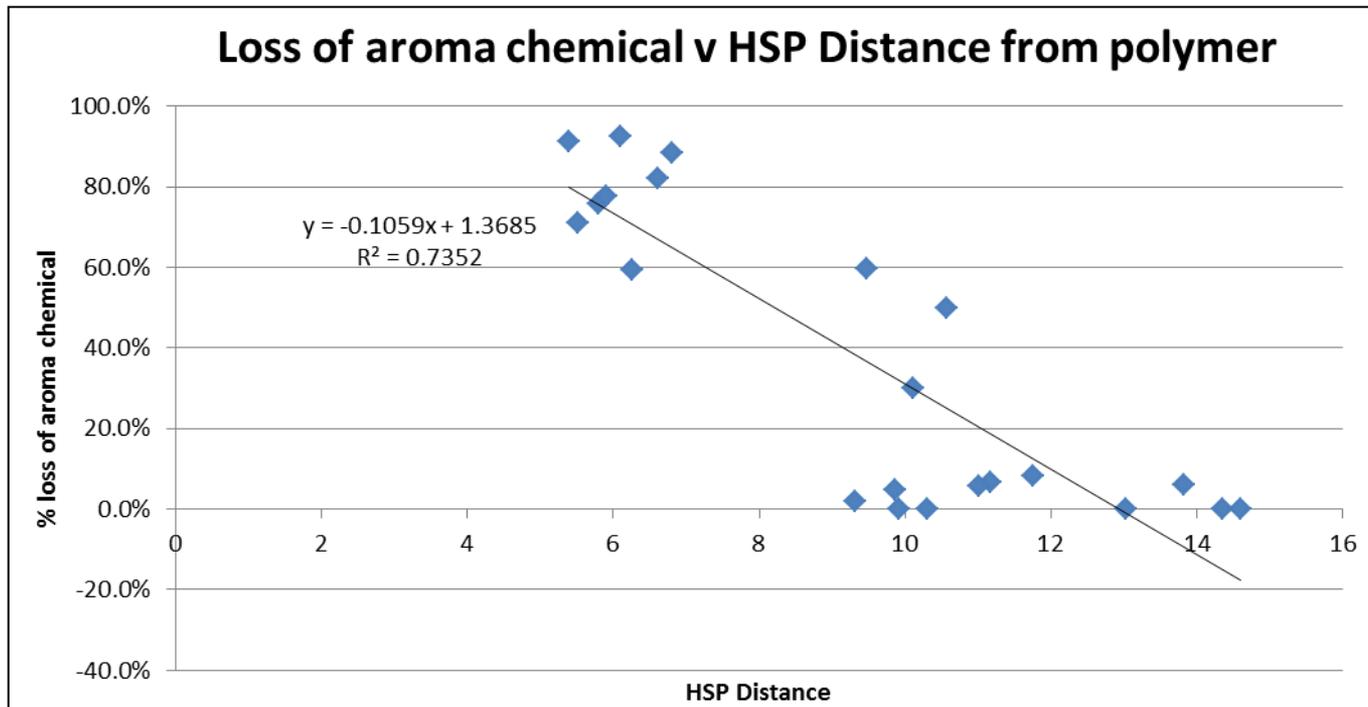
## Special Topics: Glove Selection

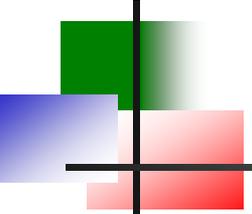
---

- **If there's interest in choosing the right gloves for a chemical, make sure there's a big HSP mismatch between chemical and glove**
  - **Rather obvious, but confirmed by large studies**
  - **A rational way to choose gloves for handling cytotoxic chemicals**
  - **Also good for handling any new chemicals with unknown properties more generally**

# Special Topics: Aromas/Fragrances

- Many aroma and fragrance HSPs are known
- Unknowns are often simple molecules, enabling accurate HSP predictions
- Flavor scalping, migration etc. explained using partition coefficients (from HSPs) and diffusion theory (depends on molecular size, shape)

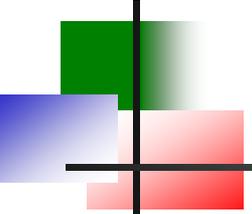




# Conclusions

---

- **HSPs represent a useful middle ground when treating solubility**
  - **Not just empirical correlations (thermodynamic basis)**
  - **Detailed enough to approximate reality much of the time**
  - **General enough to apply to a range of materials**
    - **Highly polar / charged species represent one exception**
    - **Amphiphilic species (i.e. where different interactions are localized to different parts of the molecule) represent a second exception**
  - **Determined relatively easily (depending on definition)**
- **Once HSPs are known, there are many, many applications**
  - **Finding a solvent for a new polymer or chemical**
  - **Replacing a bad solvent with greener options**
  - **Looking to cause or prevent skin permeation**
  - **Identifying appropriate personal protective equipment (PPE)**
  - **Controlling flavor scalping, migration, etc.**

A decorative graphic consisting of overlapping colored squares (green, blue, red) and a black crosshair.

# Acknowledgements

---

- **The HSPiP Team:**
  - **Prof. Steven Abbott**
    - <http://www.stevenabbott.co.uk/>
  - **Dr. Charles Hansen**
    - <http://hansen-solubility.com/>
  - **Dr. Hiroshi Yamamoto**
    - <http://www.pirika.com/>

***THANK YOU FOR YOUR ATTENTION!***